

# Consistent Mesh Parameterizations

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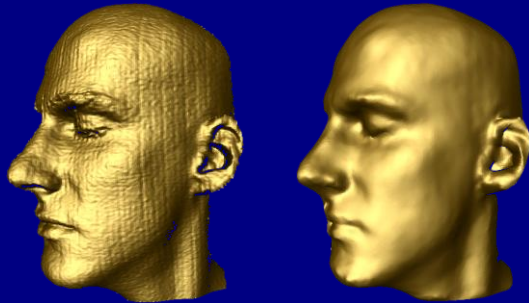
**Peter Schröder**

**Caltech**

# Motivation

## Digital Geometry Processing (DGP)

- Do for surfaces what DSP does for sound, images, and video



denoising



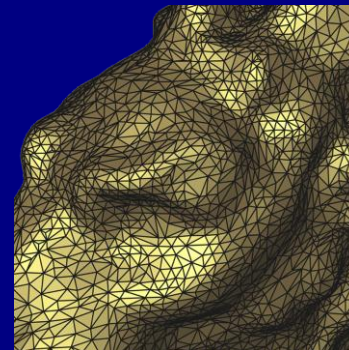
enhancement

- Requires smooth parameterizations

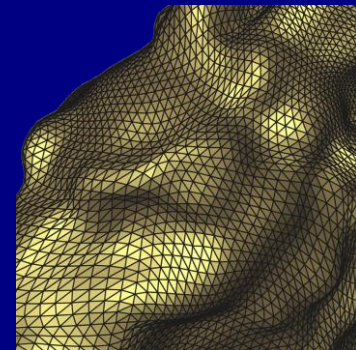
# Parameterizations

## Smooth sampling pattern

- Individual surface setting
  - *coarse mesh (base domain)*
  - *semi-regular refinement*
- Efficient algorithms



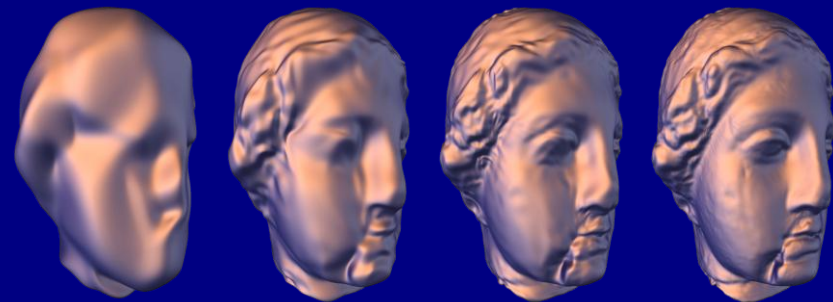
irregular



semi-regular



hierarchical editing

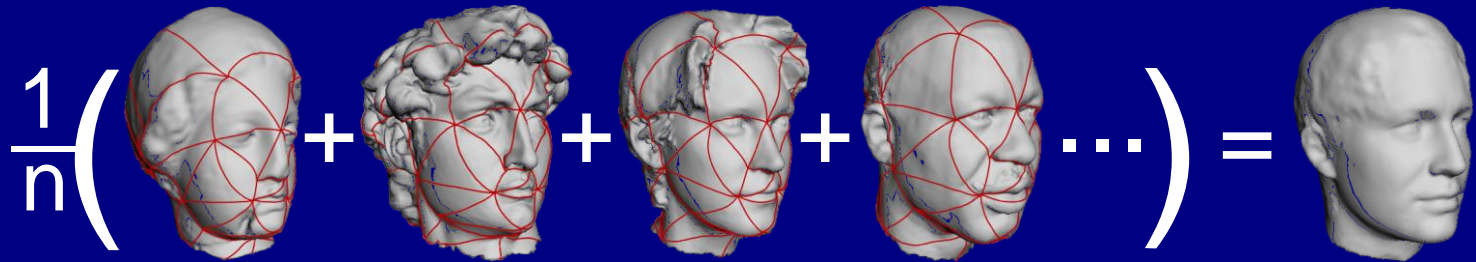


progressive transmission

# Parameterizations

## What about multiple objects?

- Computing the mean

$$\frac{1}{n} \left( \text{Mesh 1} + \text{Mesh 2} + \text{Mesh 3} + \text{Mesh 4} + \dots \right) = \text{Mean Mesh}$$


- ... and many other algorithms
  - *blending, principal components, etc.*

**Need consistent parameterizations!**

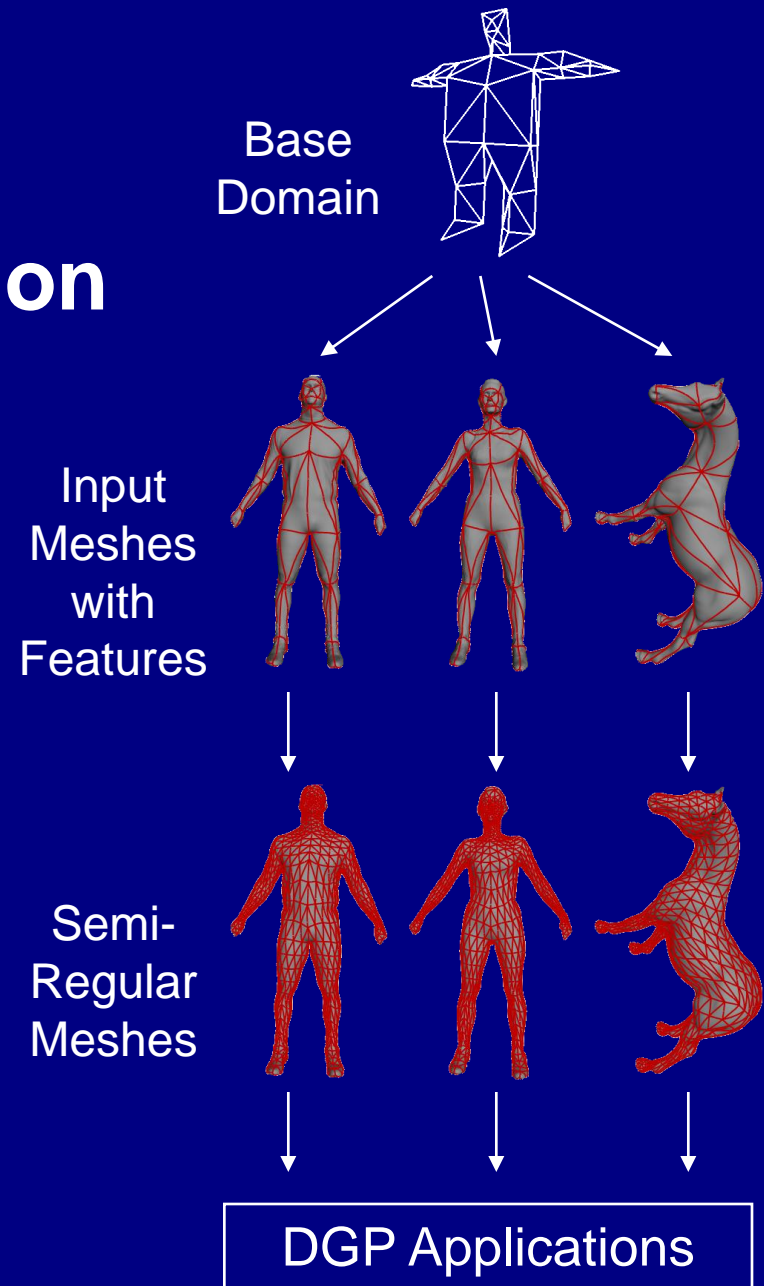
# Goal

## Consistent parameterization

- same base domain
- correspondences
  - *vertices, edges*
- smooth & fair

## Common sampling

- samples 1-1



# Previous Work

## Mesh Simplification, Progressive Meshes, ...

- [Hoppe 94-98]

## MAPS, Morphing

- [Lee 98, 99]

## Disp. Subdivision Surfaces / Normal Meshes

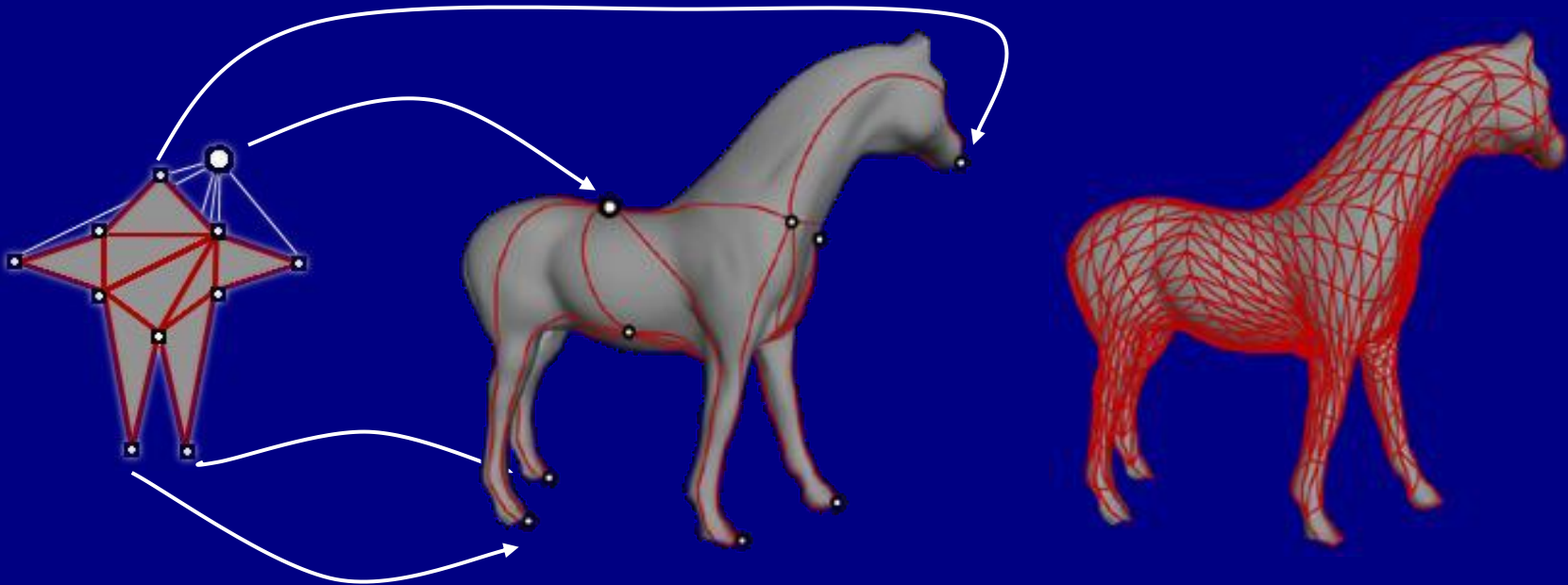
- [Lee 2000] / [Guskov 2000]

# Approach

Identify feature points (user)

Trace curves for base domain edges

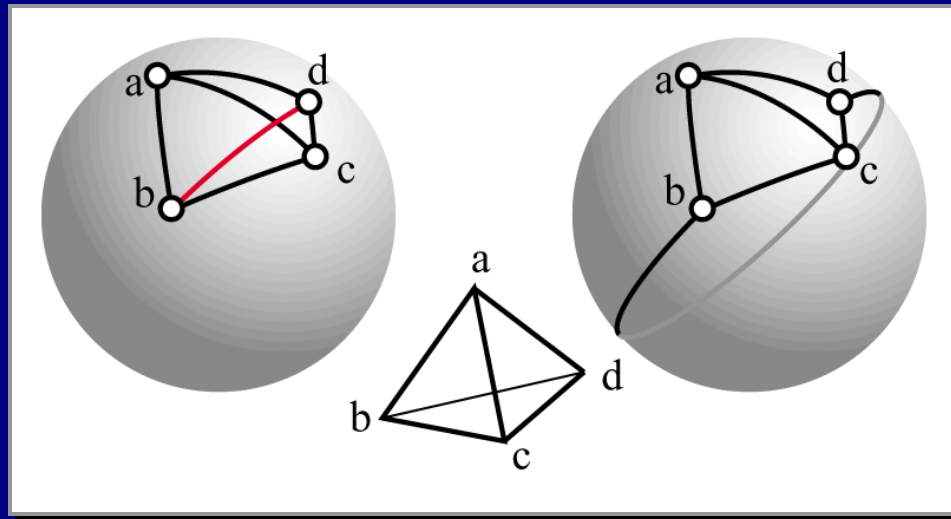
Parameterize interior of patches



# Tracing Curves

Net topologically equivalent to base domain

- Curves intersect only at vertices
- Same neighbor ordering around vertices

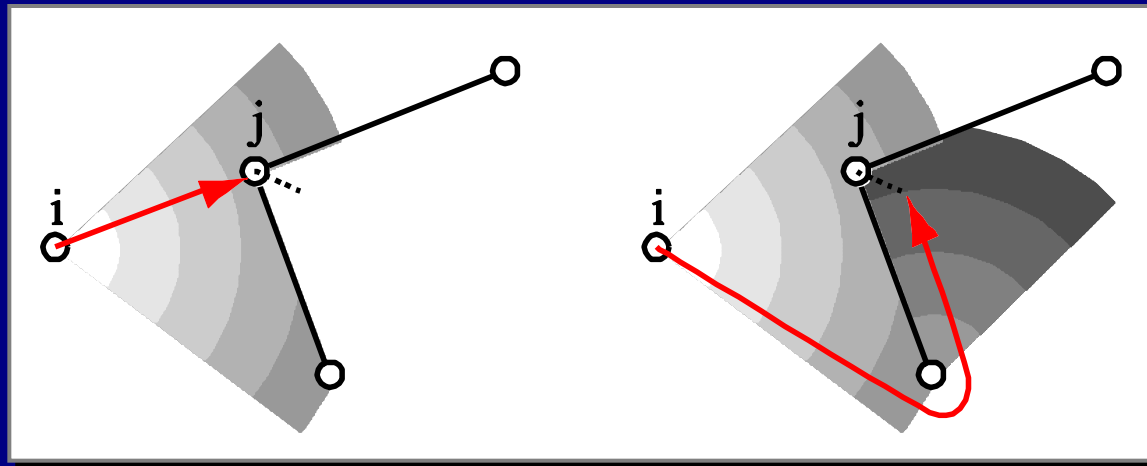




# Tracing Curves

## Restricted “brush fire” (BFS traversal):

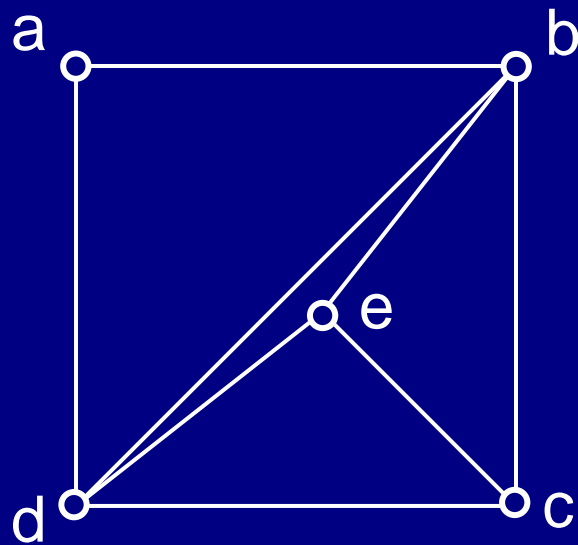
- Do not cross other curves
- Start & end in correct sector



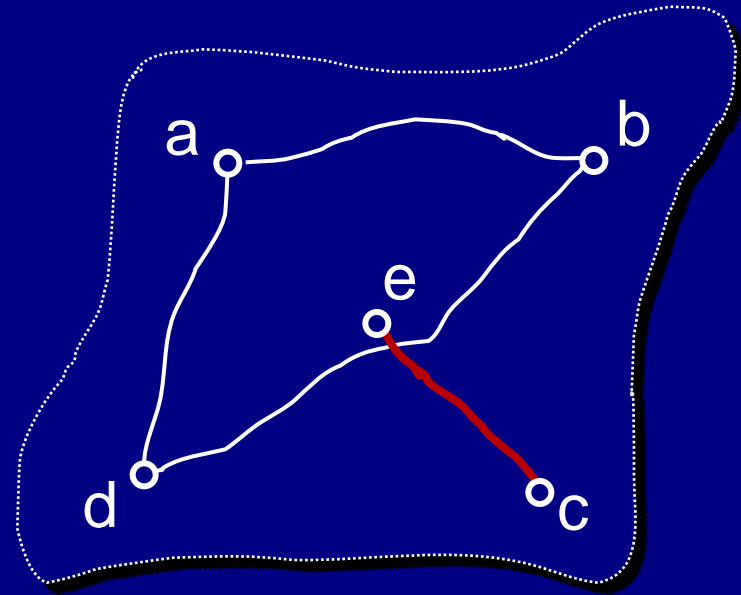
# Problem: Encircling

To avoid, first trace spanning tree

Proof of correctness in the paper



Base domain



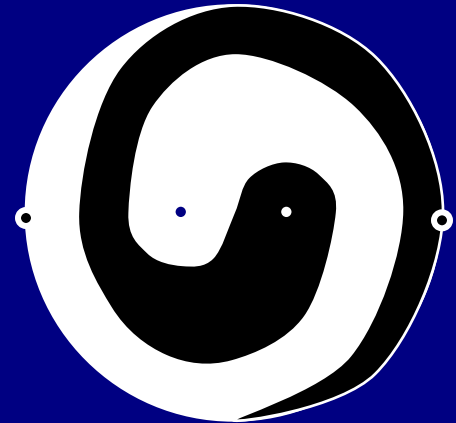
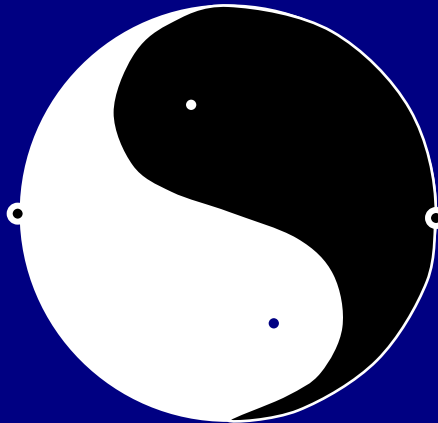
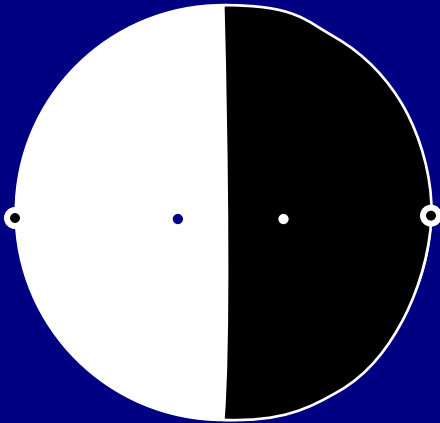
Mesh

# Topological Equivalence

**Guarantee topological equivalence of traced net and base domain**

- Trace curves w/ restricted brush fire
- Complete spanning tree before adding cycles

# Is “Topological” Enough?



# Swirl Operator

**Simple relaxation doesn't undo swirls**

**Infinity of possible configurations**

- We want the least unnecessary swirls
- Optimization very hard; use heuristics

# Heuristics

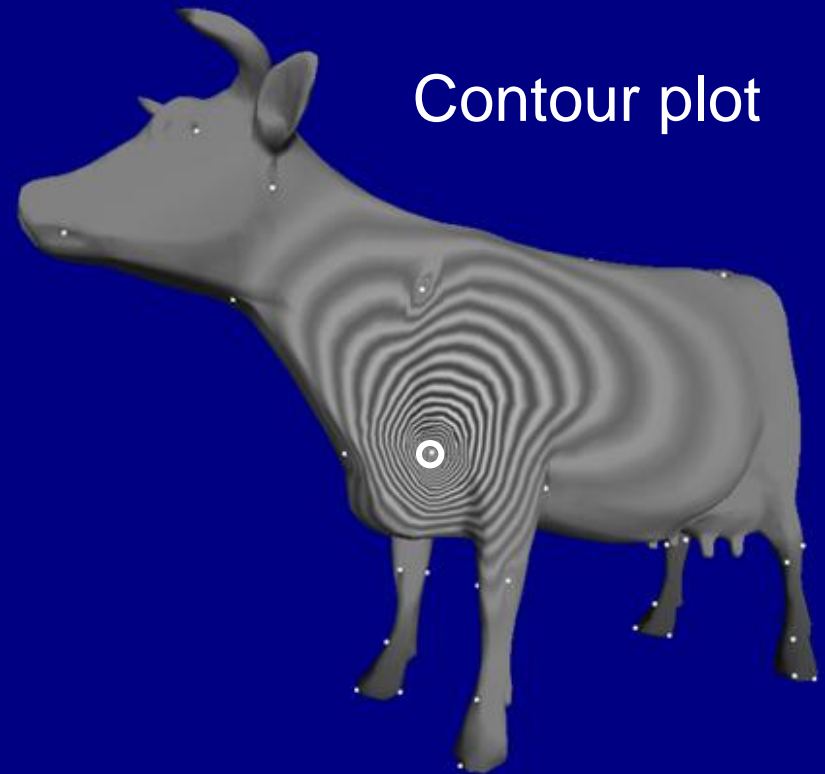
1. Feature points repel curves
2. Introduce curves in order of length
3. Delay edges of flipped triangles

# 1. Features Repel Curves

Use embedding in  $\mathfrak{R}^n$

Compute

- $I_i(k)$  = “influence” of feature  $i$  on vertex  $k$



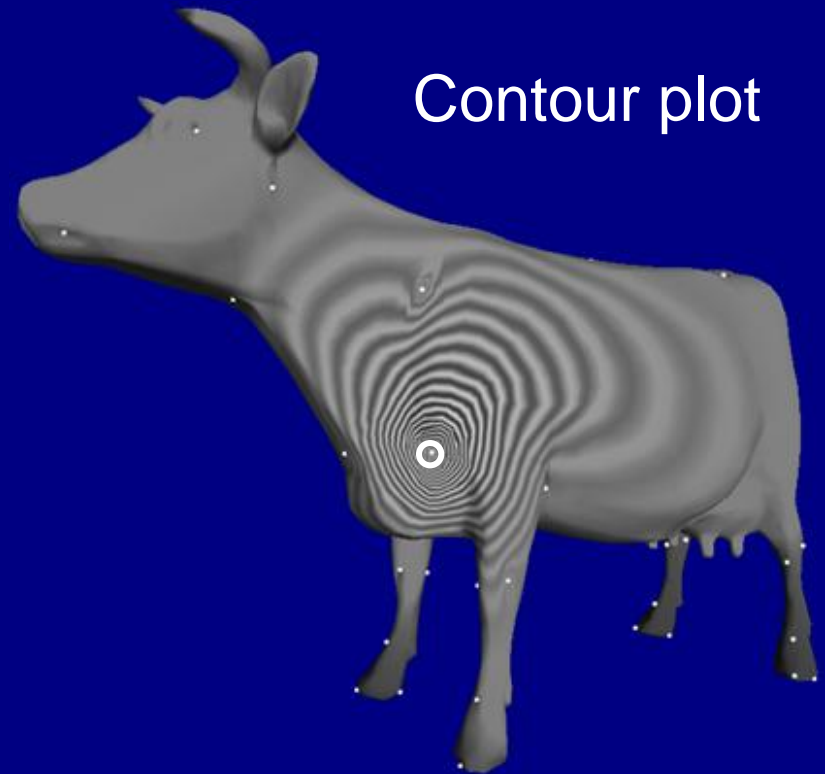
# 1. Features Repel Curves

## Initialize:

- $I_i(i) = 1$
- $I_i(\text{feature } j) = 0$

## Relax for mesh surface

- Linear system
- Floater's weights

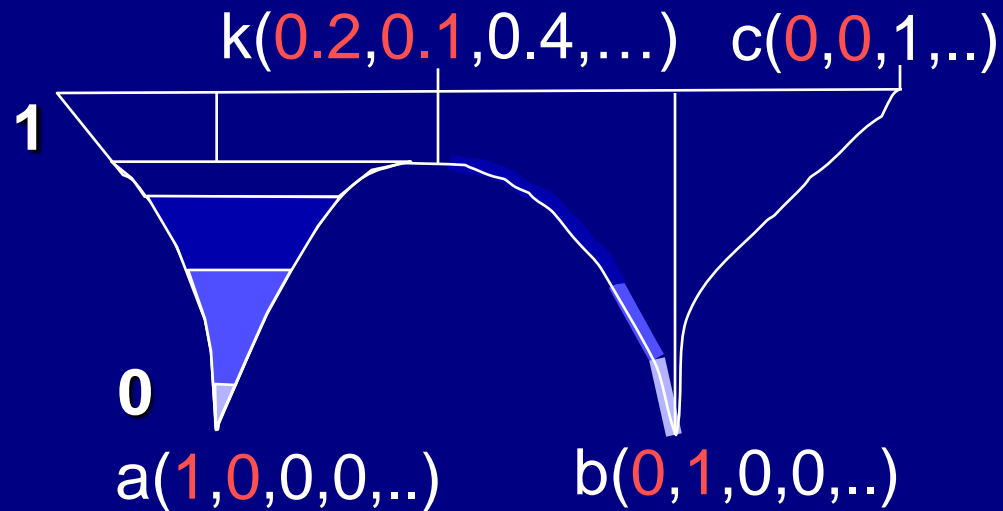
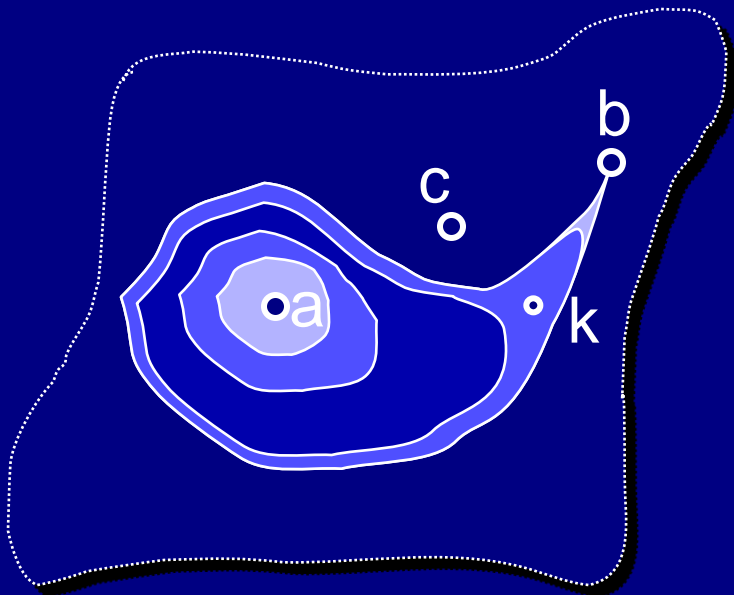




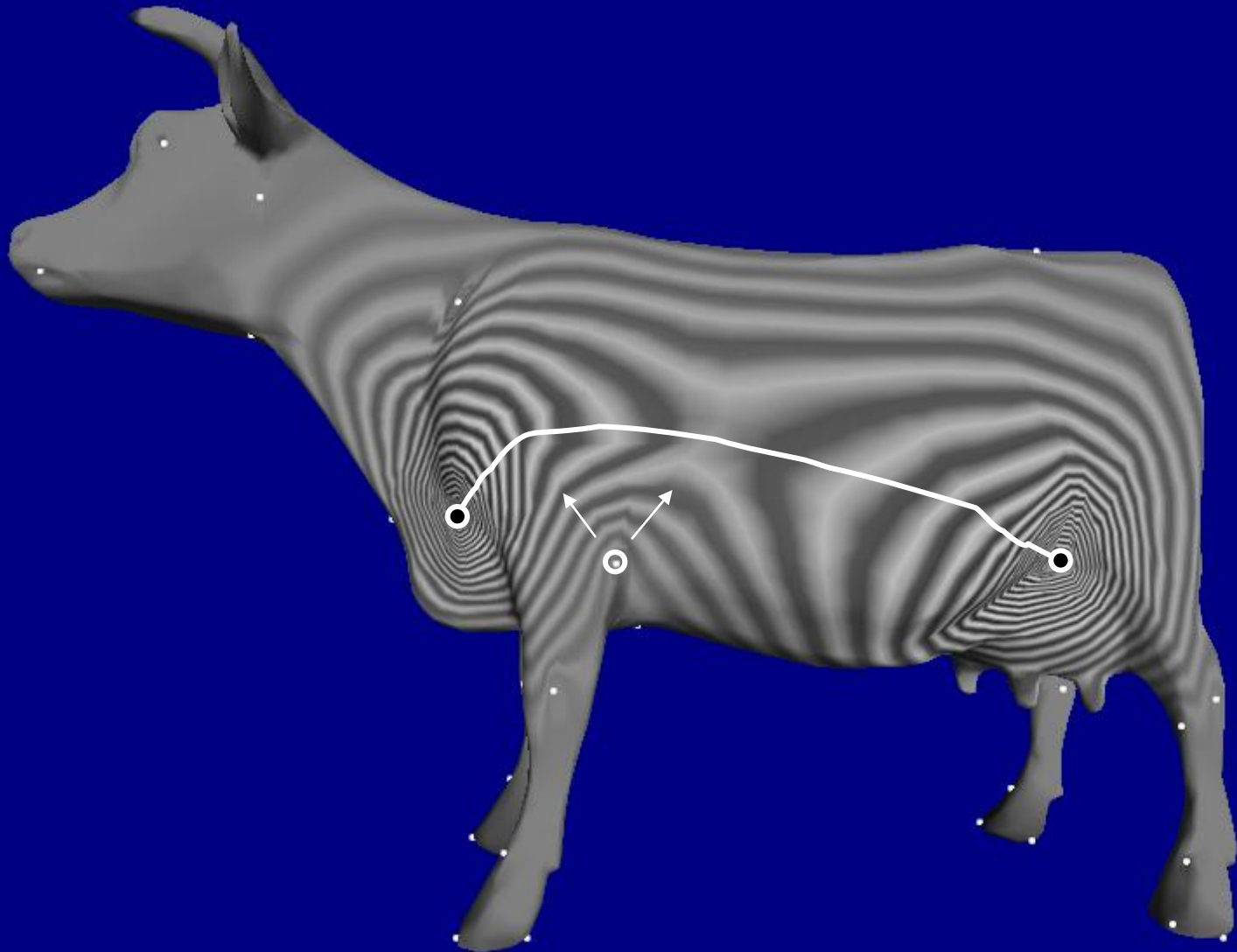
# 1. Features Repel Curves

Trace curve (a,b): brush fire with variable propagation speed

$$\text{Priority } P(k) = 1 - I_a(k) - I_b(k)$$



# 1. Features Repel Curves



## **2. Prioritize Curves by Length**

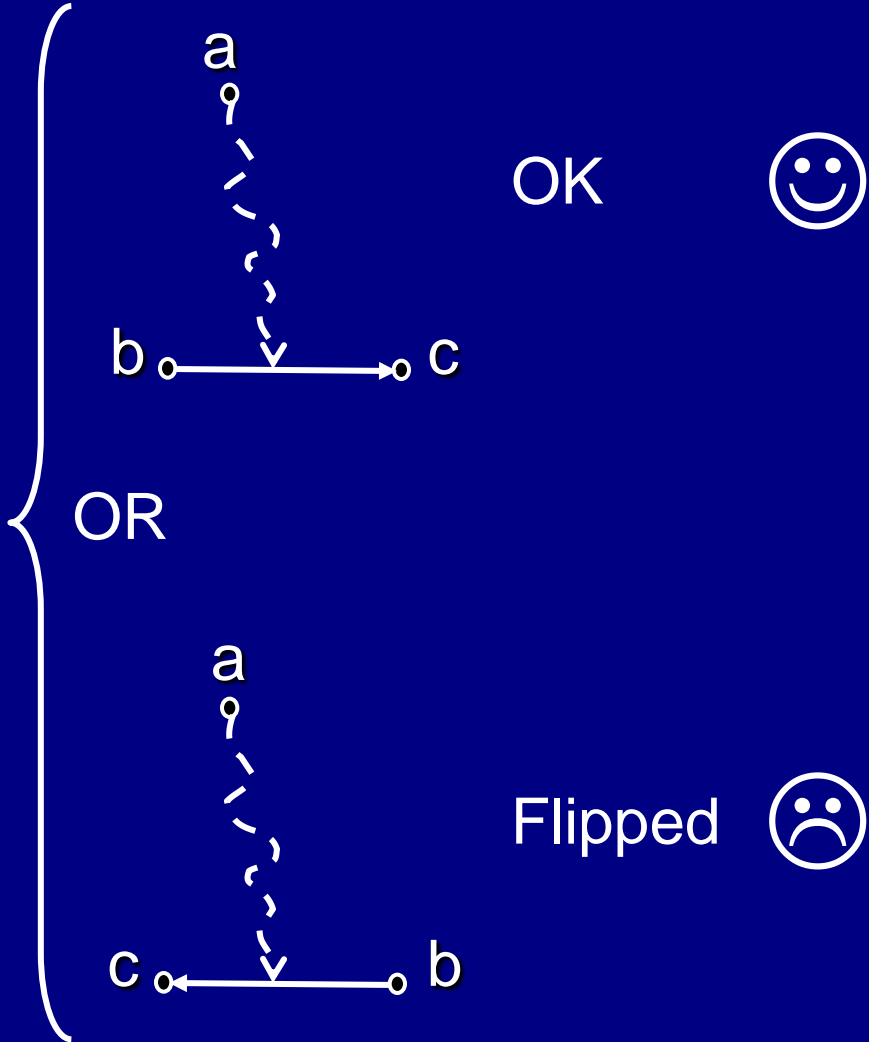
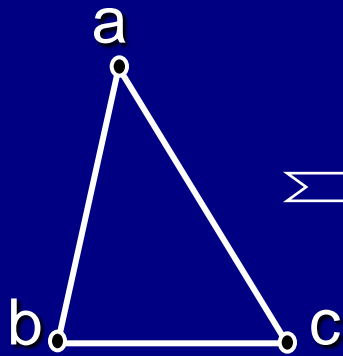
**First stage: complete spanning tree**

**Second stage: complete whole net**

**For each stage, keep priority queues**

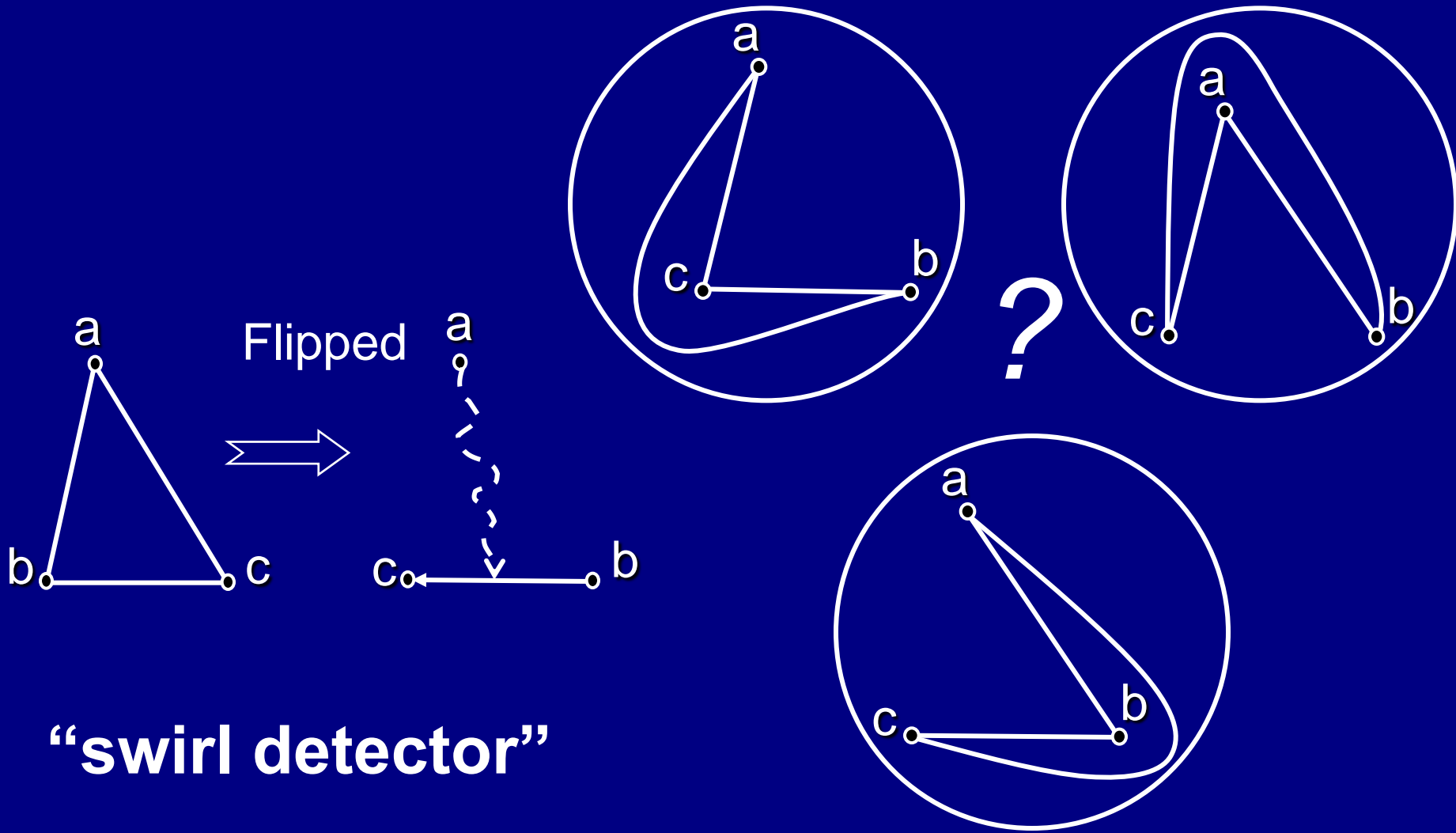
- Queues contain candidate curves
- May need to update to enforce topology

# 3. Delay Edges of Flipped Triangles

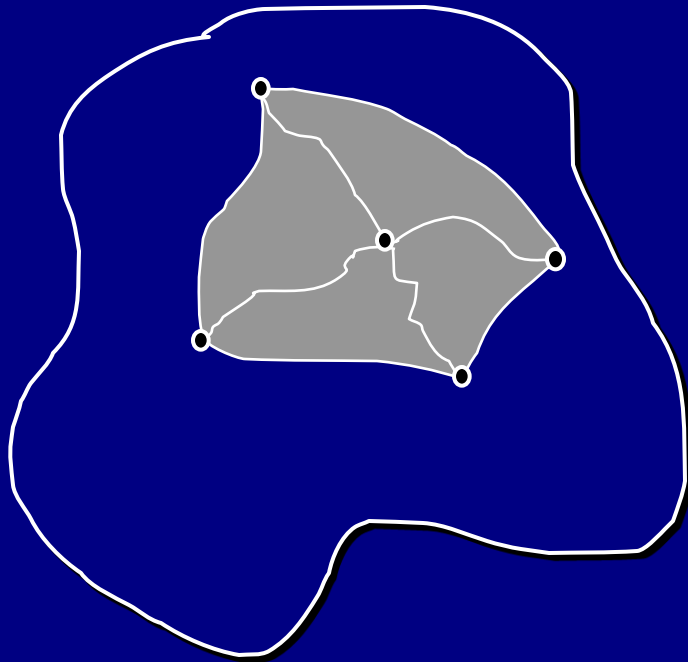


“swirl detector”

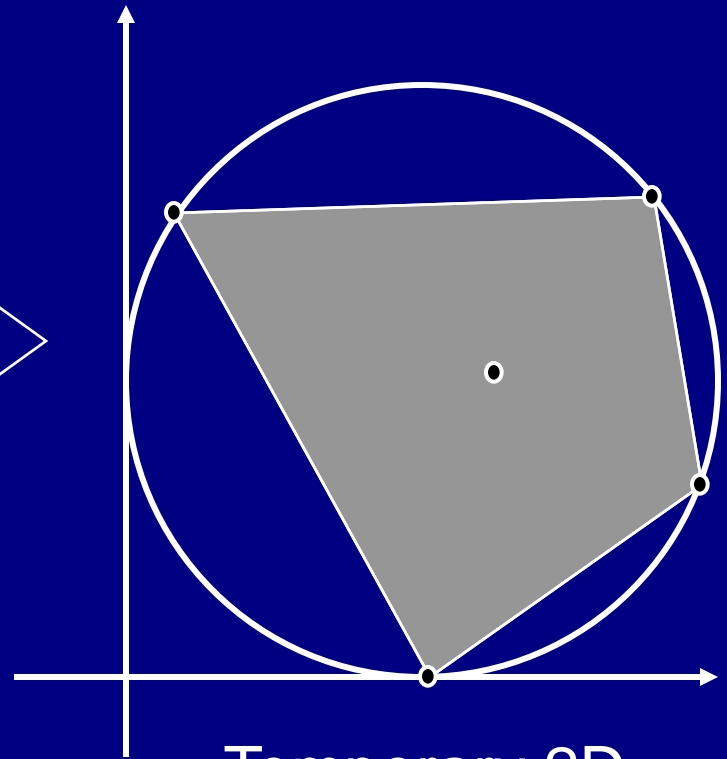
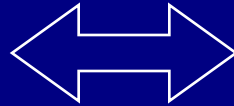
# 3. Delay Edges of Flipped Triangles



# Edge Straightening

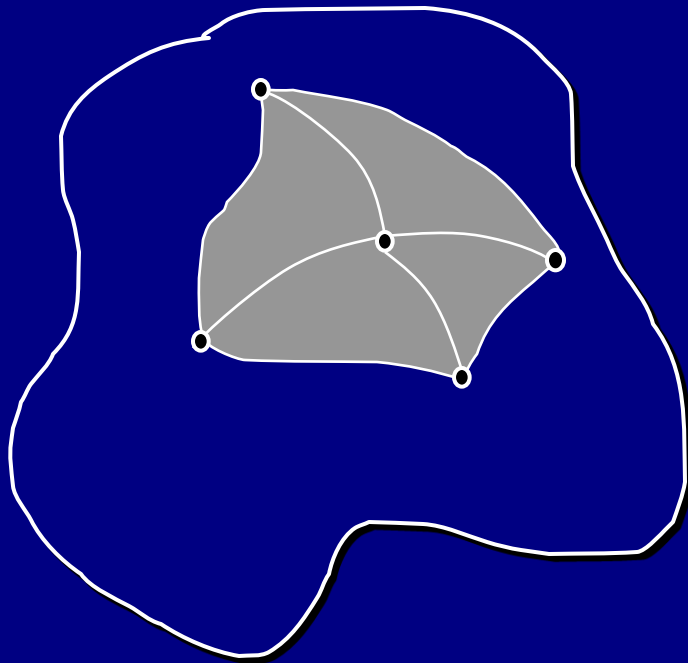


Mesh

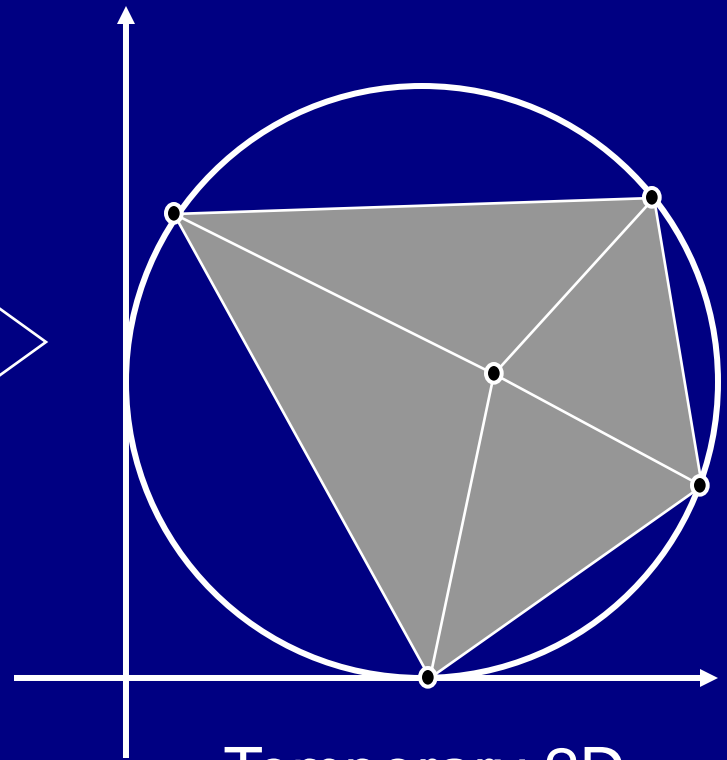
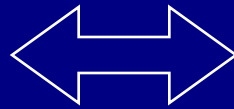


Temporary 2D  
parameterization

# Edge Straightening

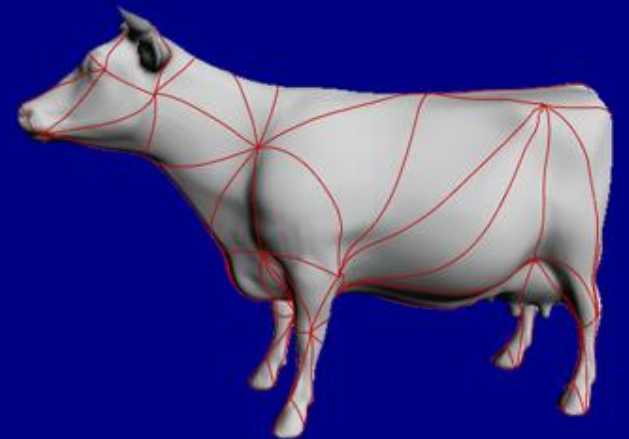
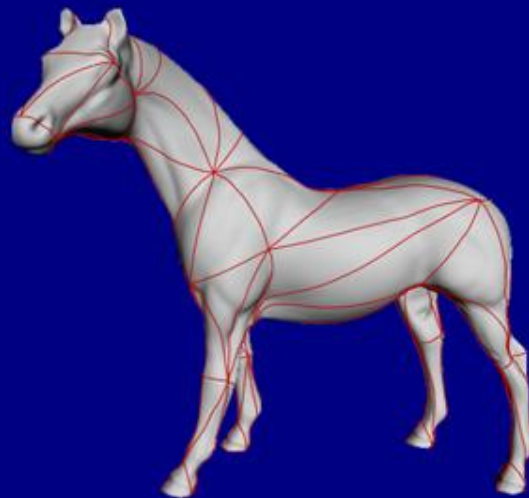
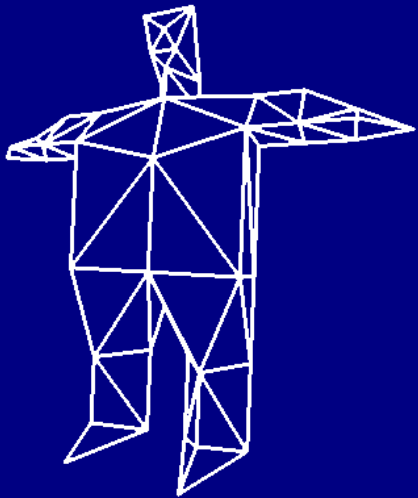
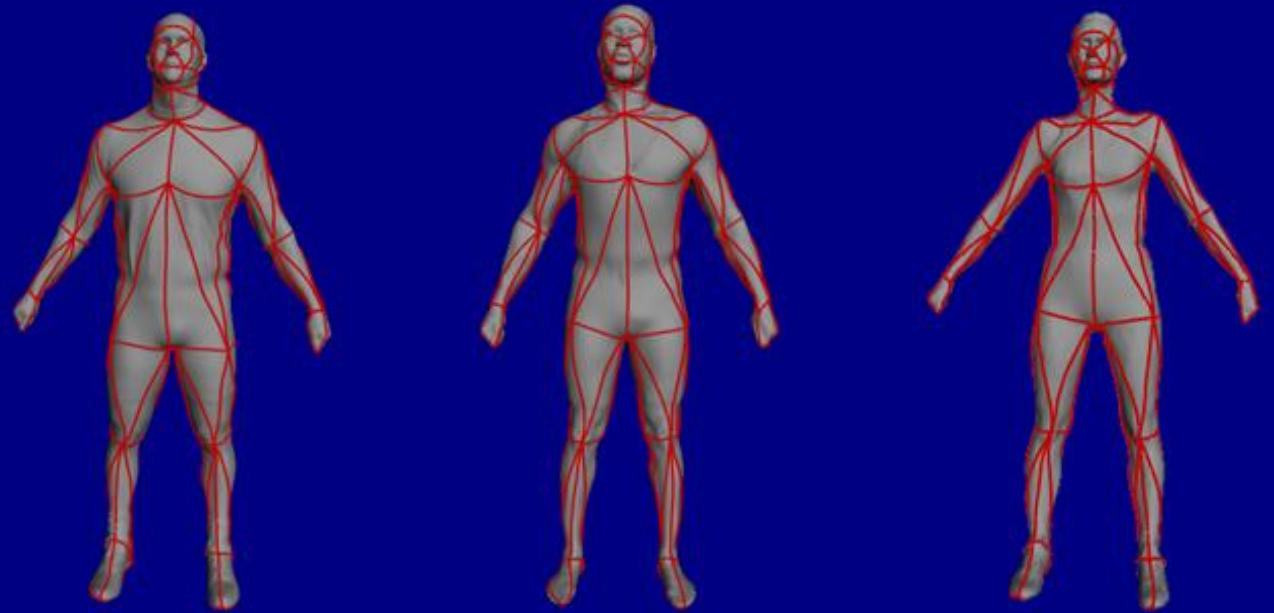


Mesh



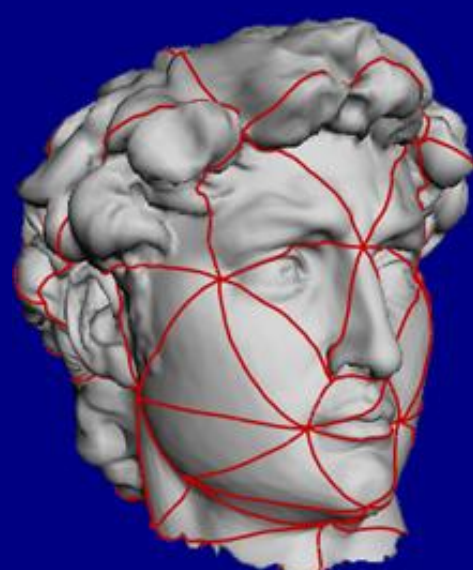
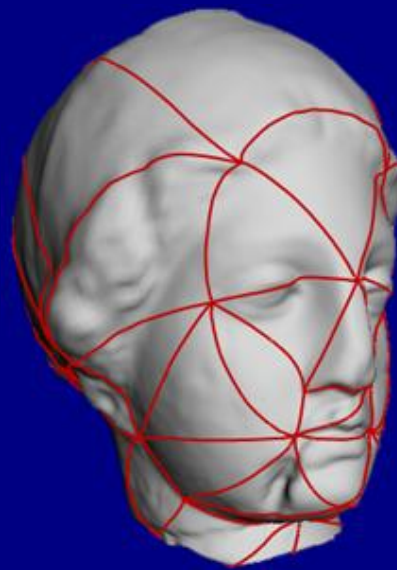
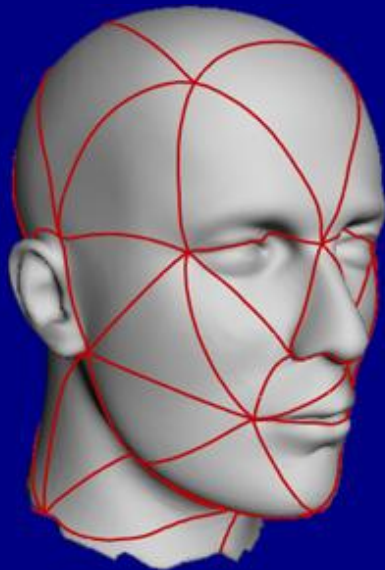
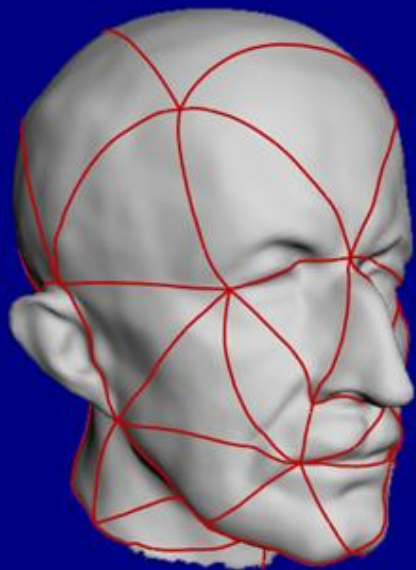
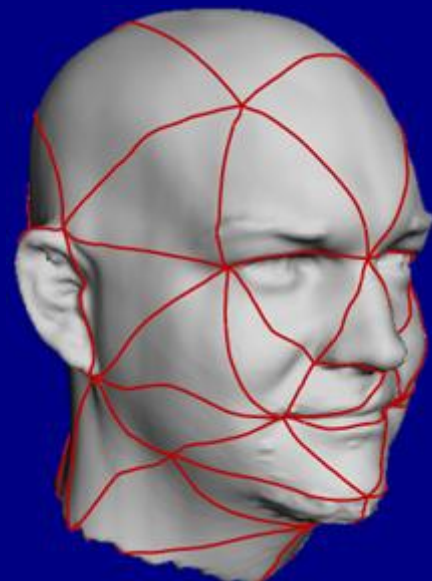
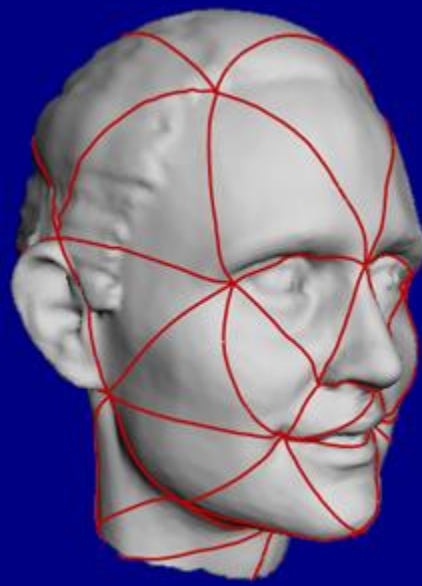
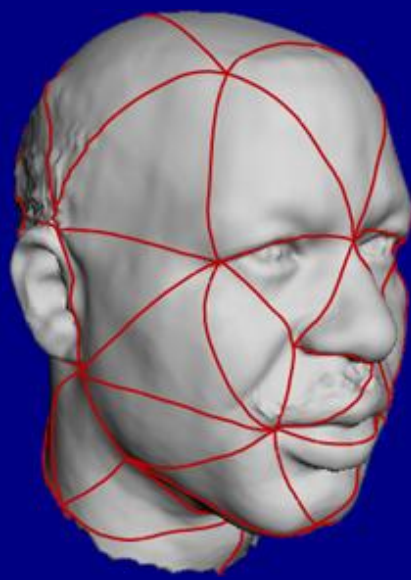
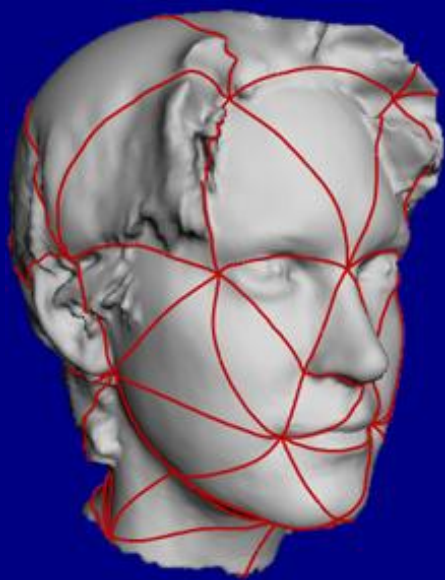
Temporary 2D  
parameterization

# Examples

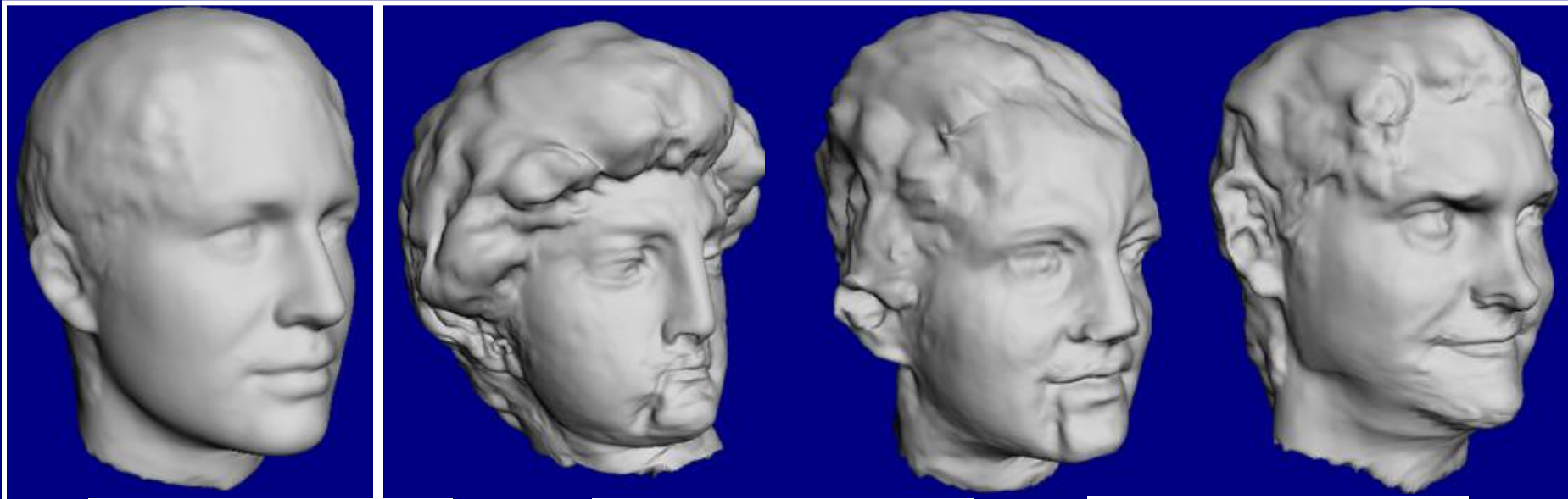




# Examples



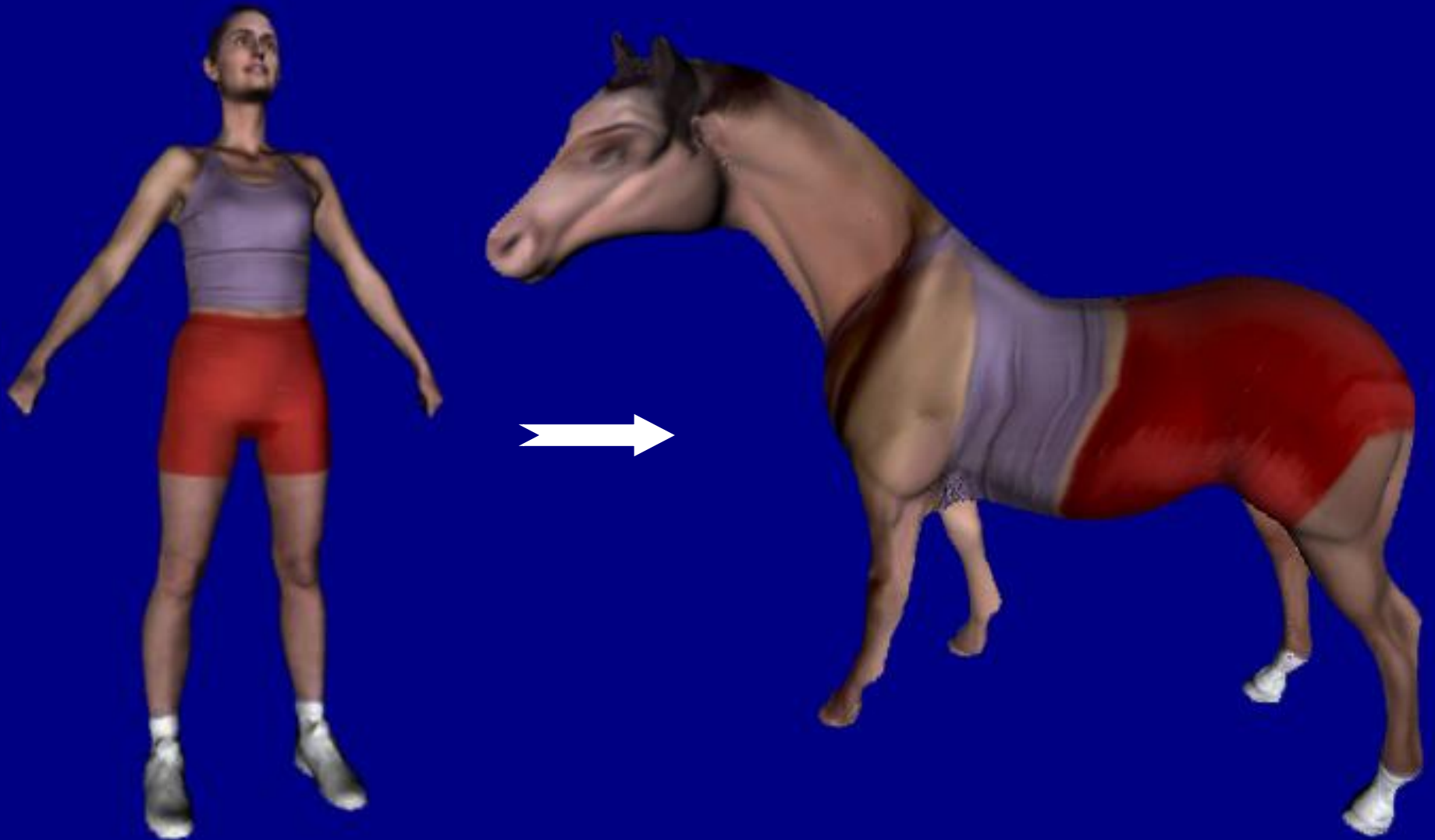
# Principal Mesh Components



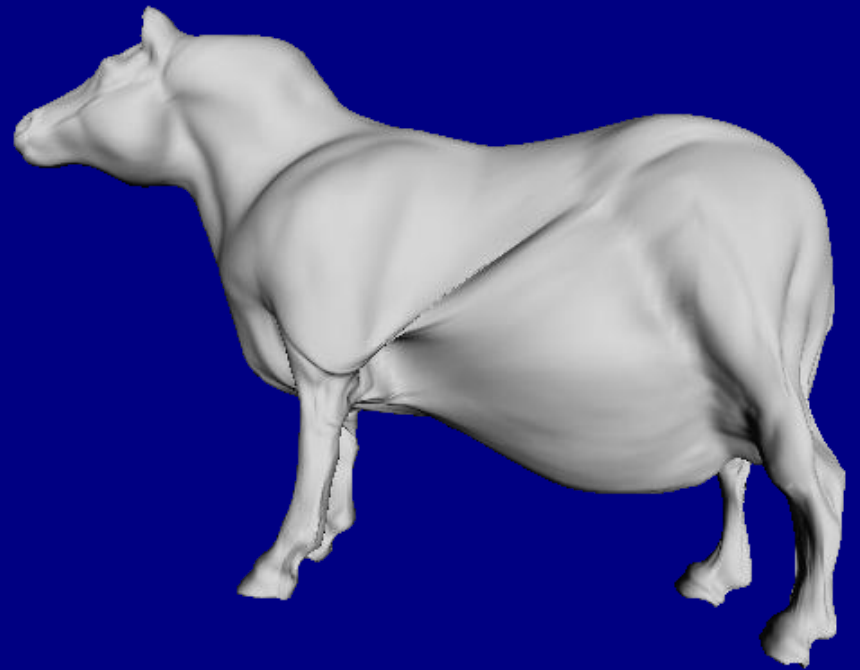
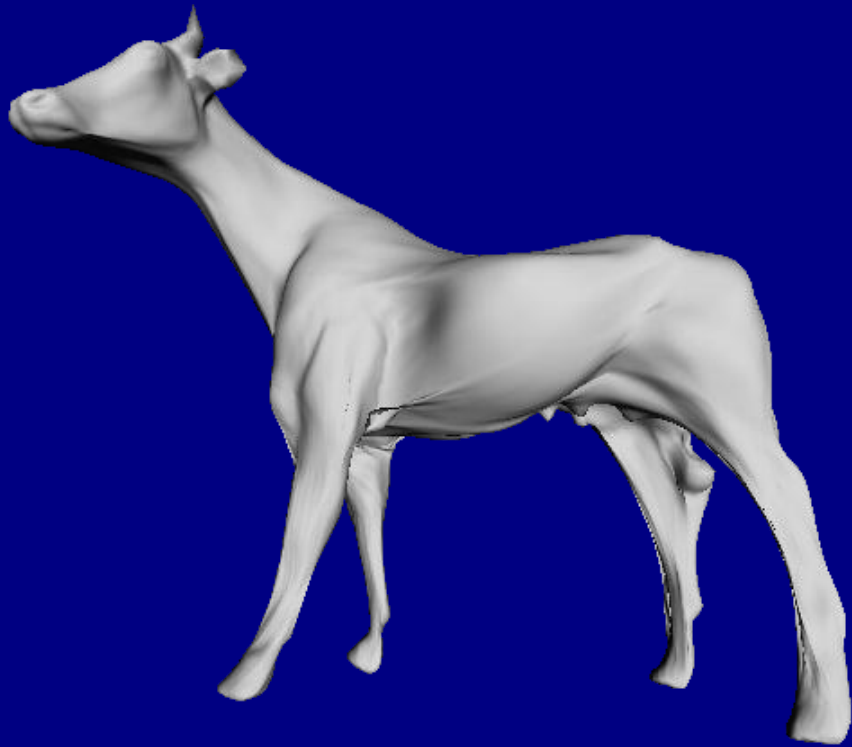
# Texture Transfer



# Texture Transfer



# Detail Transfer

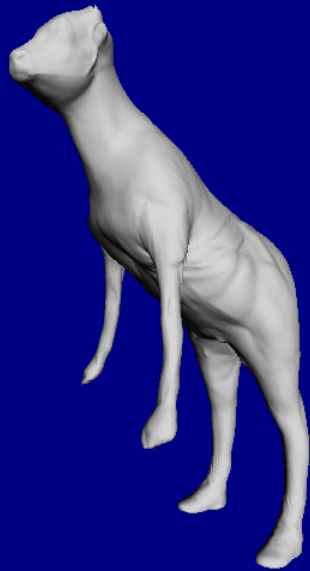


# N-way Shape Blending

Horse .33

Man .33

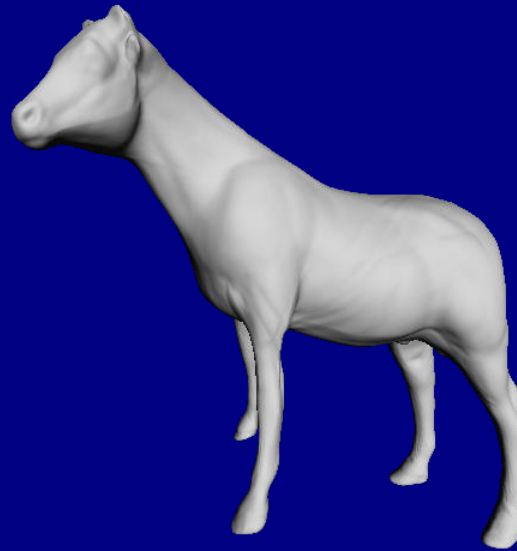
Cow .33



Horse .5

Man .25

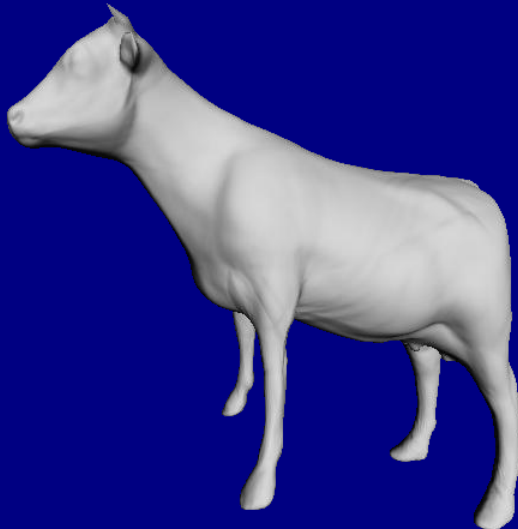
Cow .25



Horse .25

Man .25

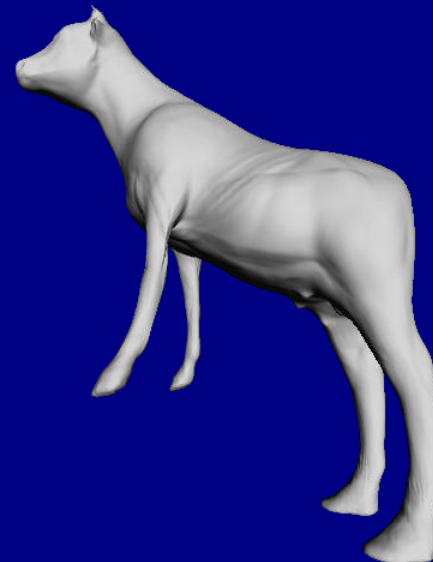
Cow .5



Horse .25

Man .5

Cow .25



# **Future Work**

**Higher genus, boundaries, missing feature points, additional feature points.**

**Transfer of animation controls**

**Use of principal component analysis for indexing and recognition in large database**

**Compression of multiple shapes**

# Acknowledgements

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**Tom Funkhouser, Lee Markosian,**

**& the Princeton crowd**